

14.7 Videos Guide

14.7a

- Definition of local maximum and local minimum values
 - If $f(a, b) \geq f(x, y)$ for all (x, y) in an open disk, then $f(a, b)$ is a local maximum
 - If $f(a, b) \leq f(x, y)$ for all (x, y) in an open disk, then $f(a, b)$ is a local minimum
- Definition of a critical point
 - A critical point is a point (a, b) in the domain of f such that $f_x(a, b) = f_y(a, b) = 0$ or one of the first partial derivatives does not exist
- Second Derivatives Test and description of a saddle point
 - Let (a, b) be a critical point of f and let
$$D(a, b) = f_{xx}(a, b)f_{yy}(a, b) - [f_{xy}(a, b)]^2$$
 - If $D < 0$, then (a, b) is a saddle point
 - If $D > 0$, then
 - if $f_{xx}(a, b) > 0$, then $f(a, b)$ is a local minimum
 - if $f_{xx}(a, b) < 0$, then $f(a, b)$ is a local maximum
 - If $D = 0$, then the Second Derivatives Test is inconclusive

14.7b

Exercise:

- Find the local maximum and minimum values and saddle point(s) of the function. Then graph the surface using a window that shows these characteristics.
$$f(x, y) = xye^{-(x^2+y^2)/2}$$

14.7c

- Absolute extrema
 - If $f(a, b) \geq f(x, y)$ for all (x, y) in the domain of f , then $f(a, b)$ is the absolute maximum
 - If $f(a, b) \leq f(x, y)$ for all (x, y) in the domain of f , then $f(a, b)$ is the absolute minimum

Exercise:

- Find the absolute maximum and minimum values of f on the set D .
$$f(x, y) = x + y - xy; \quad D \text{ is the closed triangular region with vertices } (0, 0), (0, 2), \text{ and } (4, 0).$$